

# **RAFSet 3D-2D motion estimation**

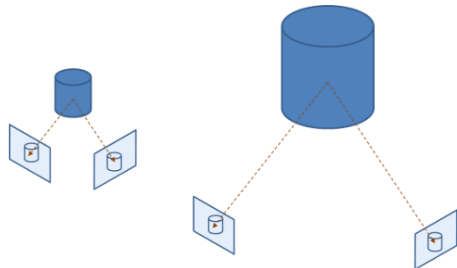
**part 1. LiDAR interpolation**

Jeon Hyun Ho

# Intro

- **Frame to frame motion estimation method**

- 2D-2D motion estimation ( Scale problem )
- ✓ 3D-2D motion estimation ( minimize image reprojection error )
- 3D-3D motion estimation ( minimize feature position error )



Scale problem

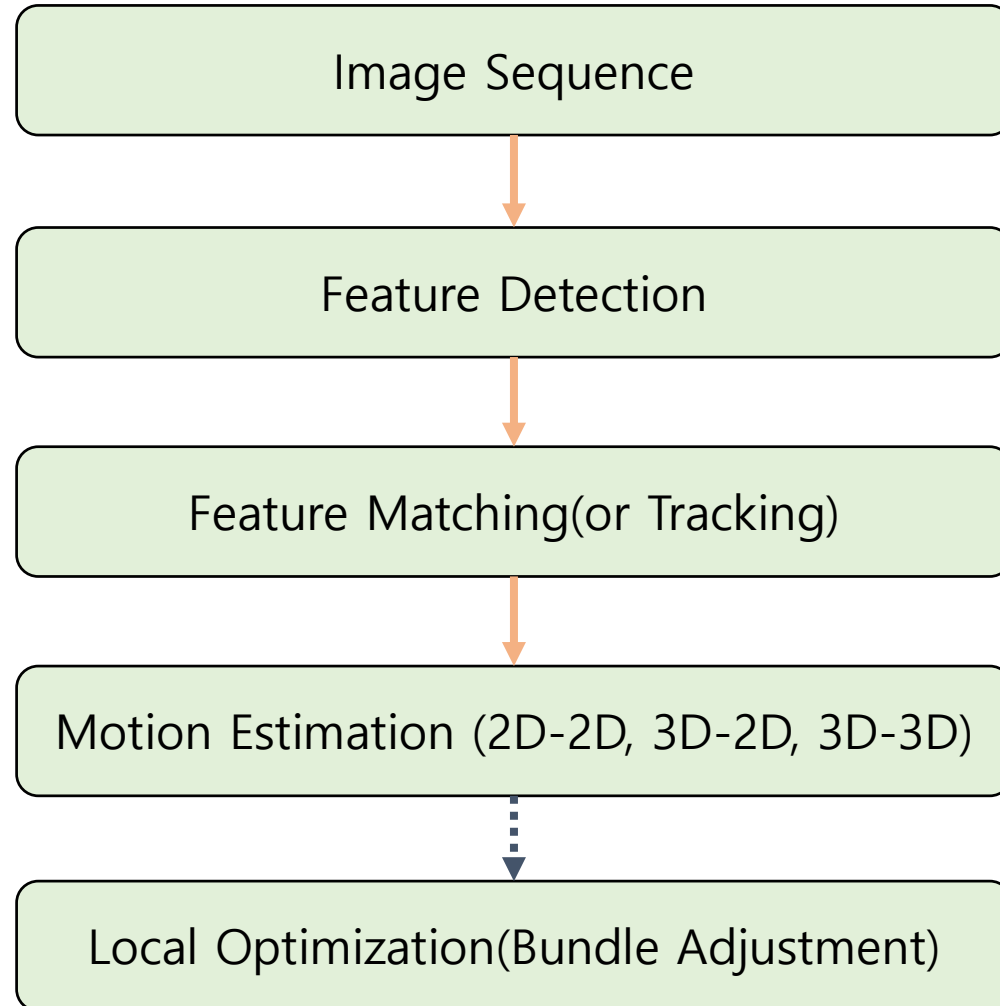


Scaramuzza, Davide, and Friedrich Fraundorfer. "Visual odometry [tutorial]." *IEEE Robotics & Automation Magazine* 18.4 (2011): 80-92.

Fraundorfer, Friedrich, and Davide Scaramuzza. "Visual odometry: Part II: Matching, robustness, optimization, and applications." *IEEE Robotics & Automation Magazine* 19.2 (2012): 78-90.

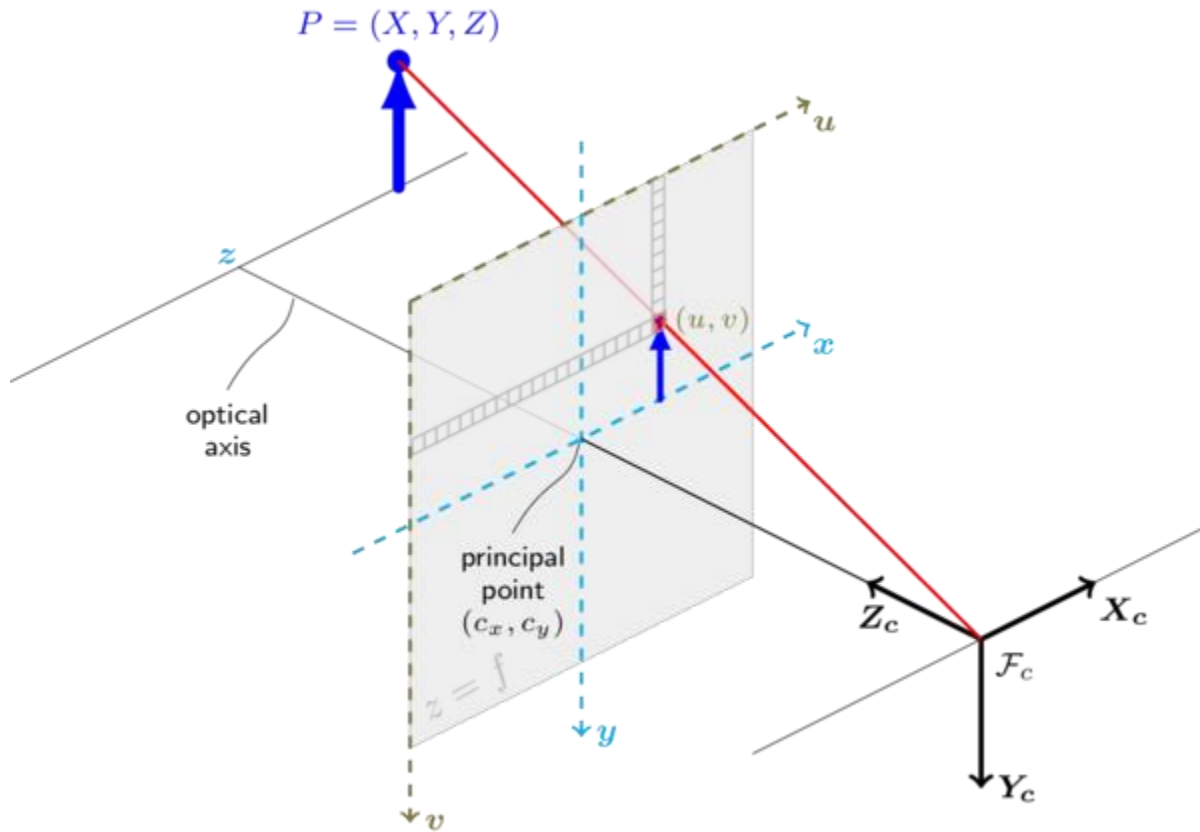
# Intro

- Feature based motion estimation process



# Interpolation

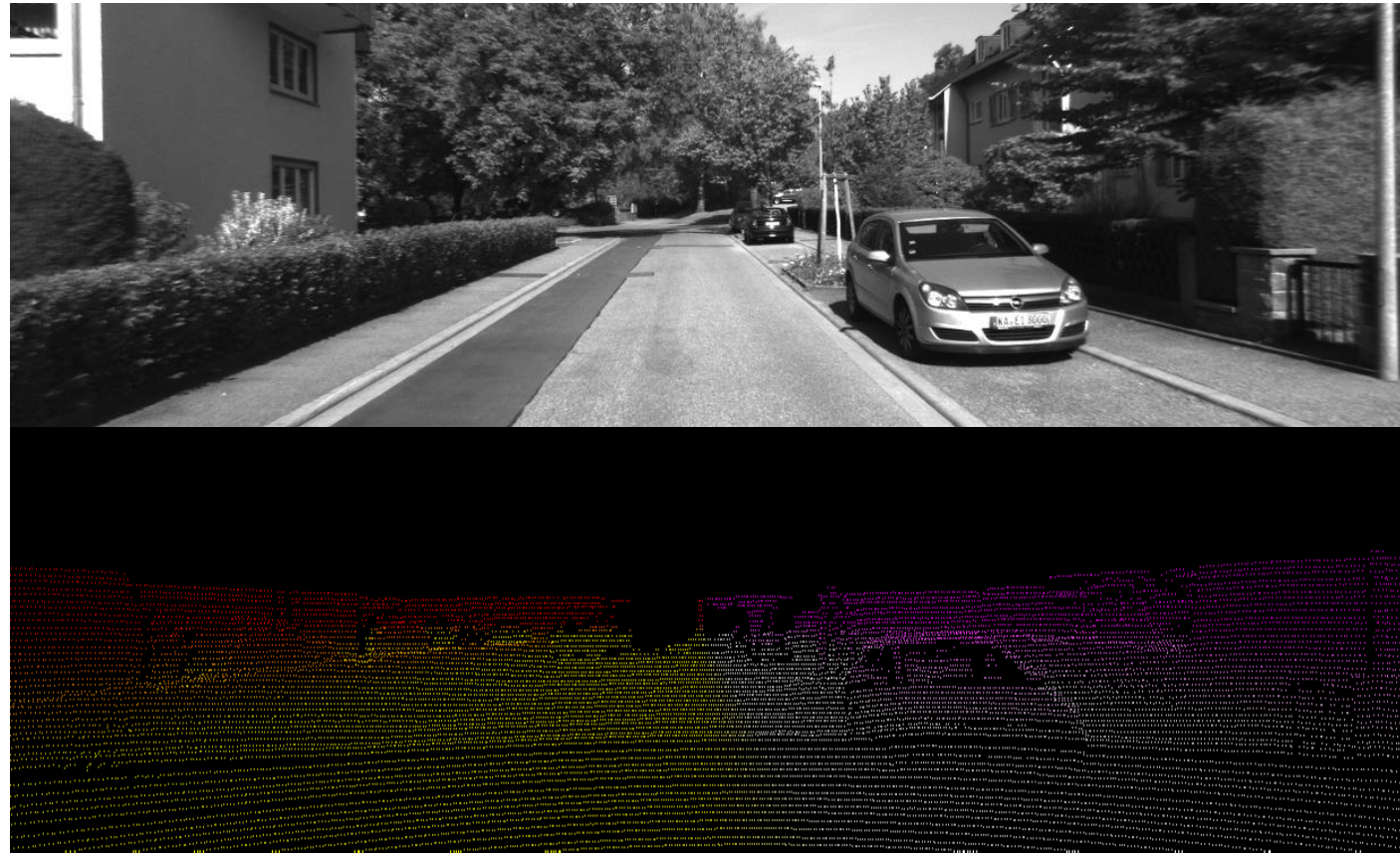
- 3D-2D motion estimation



$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

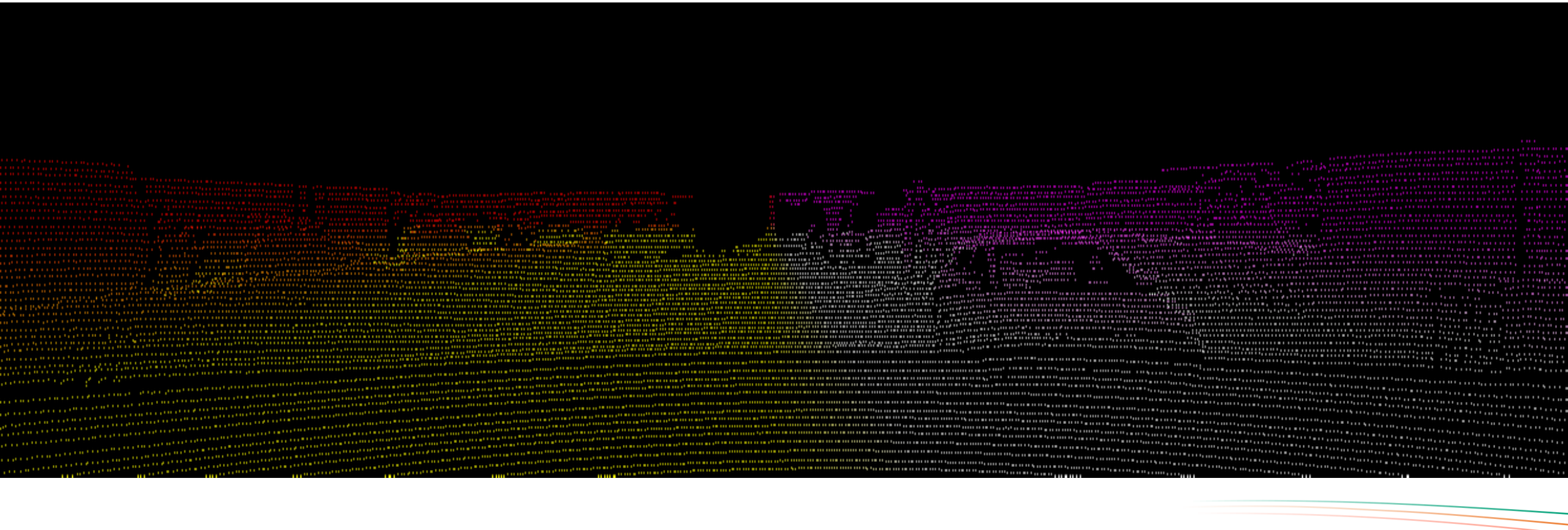
# Interpolation

- 3D-2D motion estimation
  - Sparse LiDAR data



# Interpolation

- 3D-2D motion estimation
  - Sparse LiDAR data



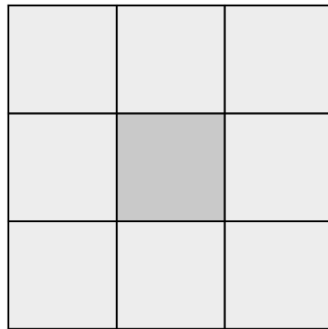
# Interpolation

- Method 1

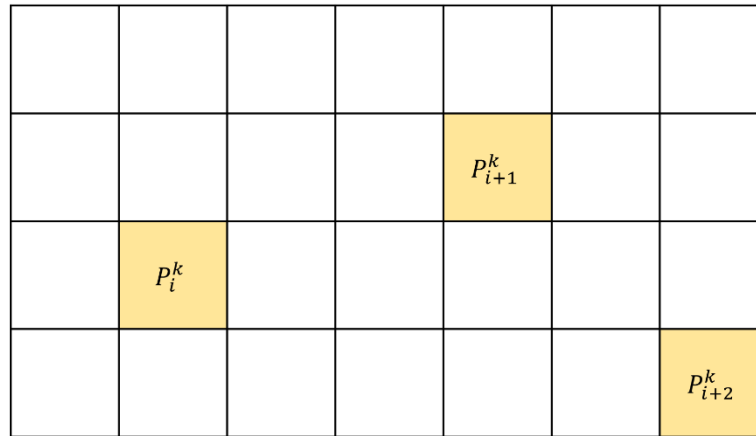
- Dilation interpolation

$$S_j = (p_i^k \oplus B)$$

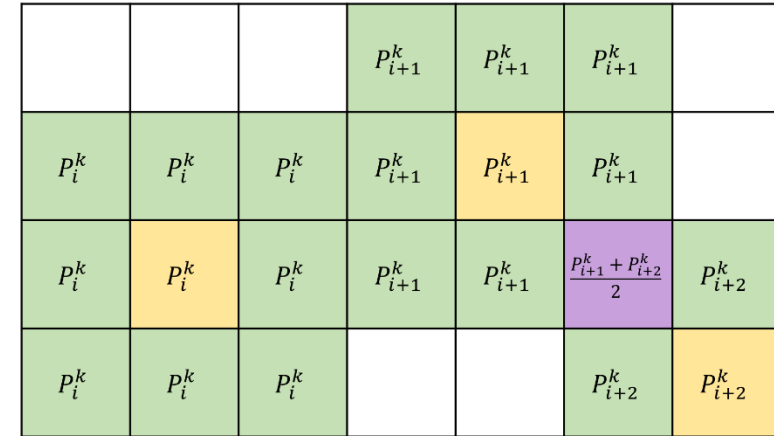
$$S_j \leftarrow P_i^k$$



B



LiDAR image

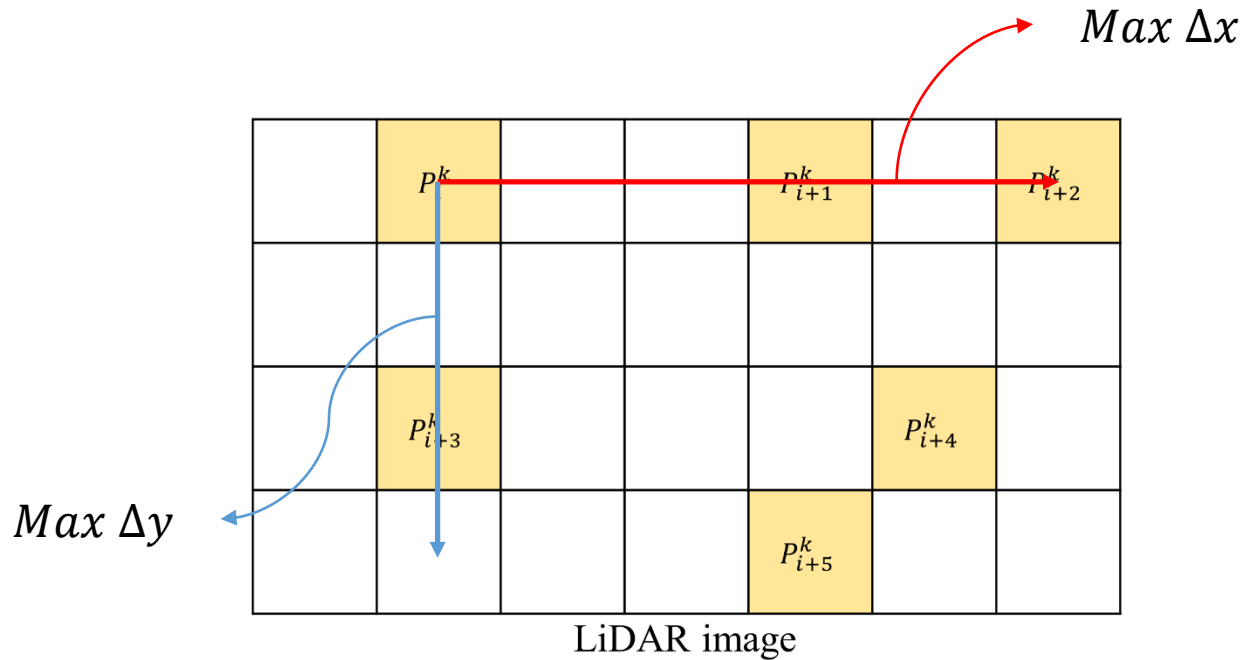


Interpolated LiDAR image

# Interpolation

- Method 2

- Adaptive bilinear interpolation\* ( $Max \Delta x$ ,  $Max \Delta y$ )



$$\text{Interpolated Point : } P^k = G * \Delta x + P_i^k$$

$$\text{Gradient : } G = \frac{P_i^k - P_{i+1}^k}{\Delta x_i^{i+1}}$$



# Interpolation

- Method 2

- Adaptive bilinear interpolation\* ( $Max \Delta x$ ,  $Max \Delta y$ )

	$P_i^k$			$P_{i+1}^k$		$P_{i+2}^k$
	$P_{i+3}^k$				$P_{i+4}^k$	
				$P_{i+5}^k$		

LiDAR image

Interpolated Point :  $P^k = G * \Delta x + P_i^k$

$$\text{Gradient : } G = \frac{P_i^k - P_{i+1}^k}{\Delta x_i^{i+1}}$$

# Interpolation

- Method 2

- Adaptive bilinear interpolation\* ( $Max \Delta x$ ,  $Max \Delta y$ )

	$P_i^k$			$P_{i+1}^k$		$P_{i+2}^k$
	$P_{i+3}^k$				$P_{i+4}^k$	
				$P_{i+5}^k$		

LiDAR image

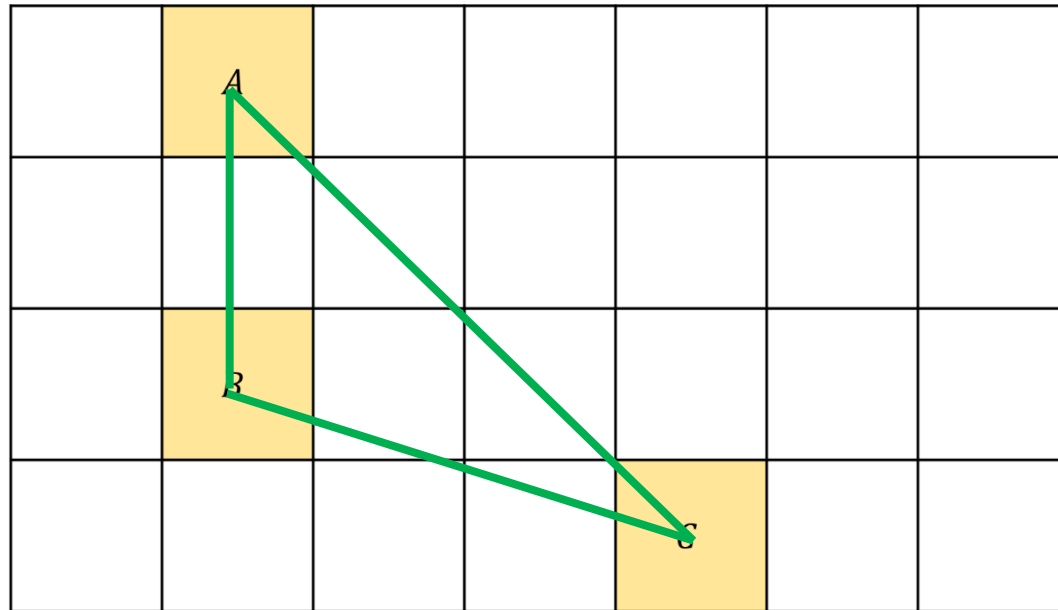
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# Interpolation

- Method 3

- Plane interpolation

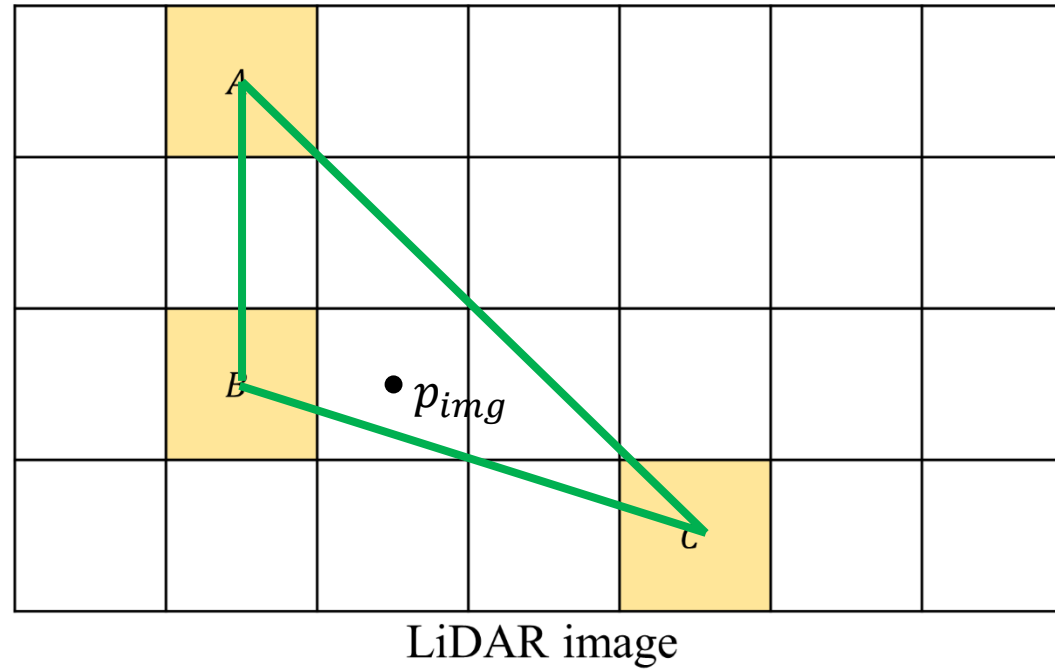


LiDAR image

$$\left. \begin{array}{l} A(X_A, Y_A, Z_A) \\ B(X_B, Y_B, Z_B) \\ C(X_C, Y_C, Z_C) \end{array} \right\} \text{Plane } ABC$$

# Interpolation

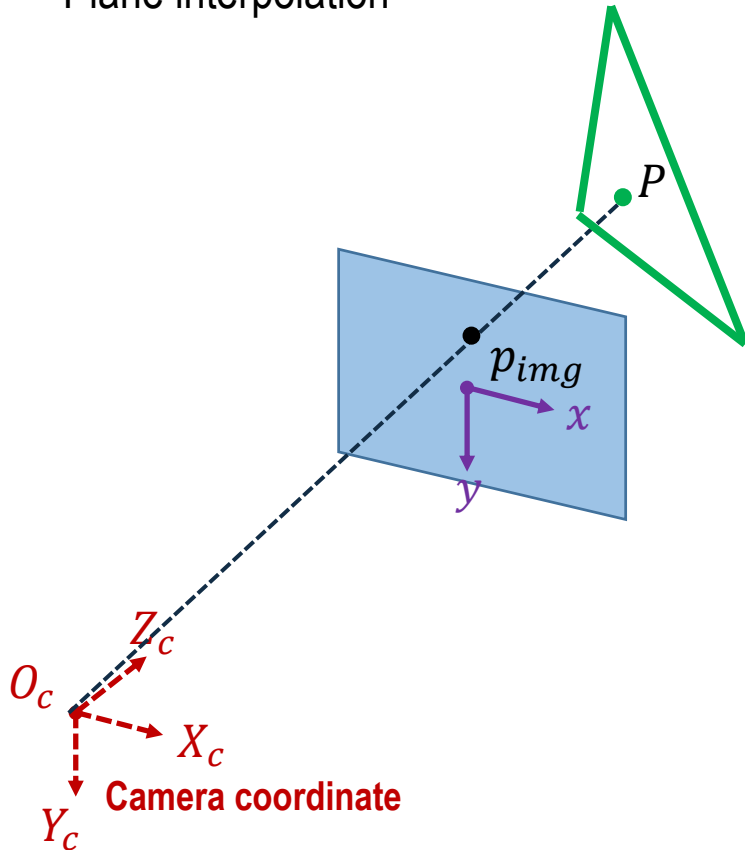
- Method 3
  - Plane interpolation



# Interpolation

- Method 3

- Plane interpolation

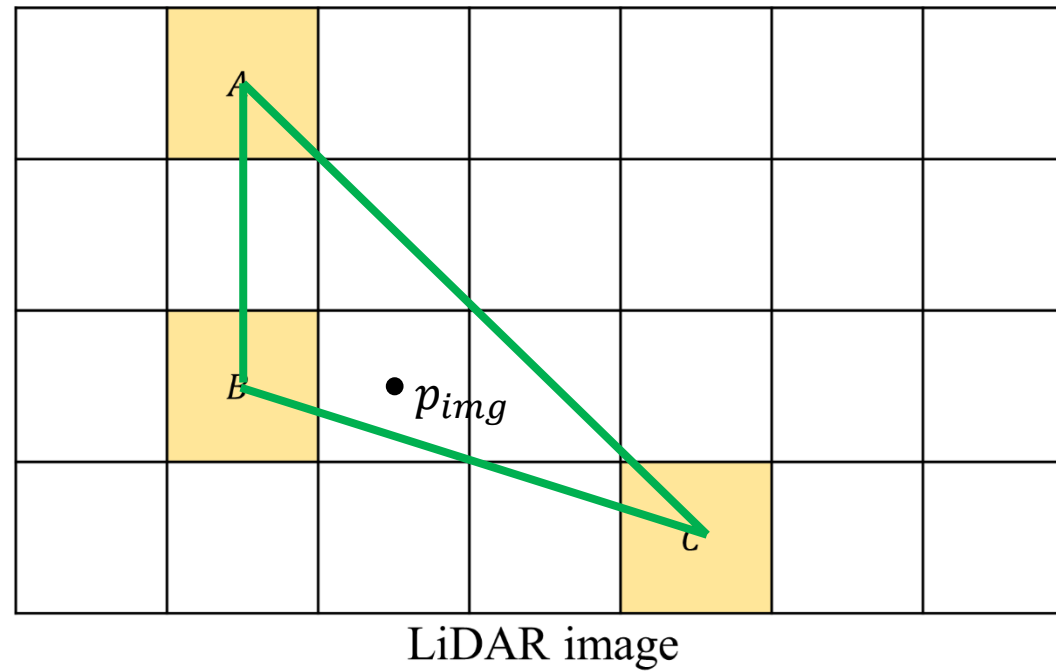


$$\begin{aligned} & p_{img}^{2D}(x, y) \\ & \downarrow \\ & p_{img}^{2D}(x - u, y - v) \\ & \downarrow \\ & p_{img}^{3D}(x - u, y - v, f) \\ & \downarrow \\ & line(O_c, p_{img}^{3D}) \end{aligned}$$

# Interpolation

- Method 3

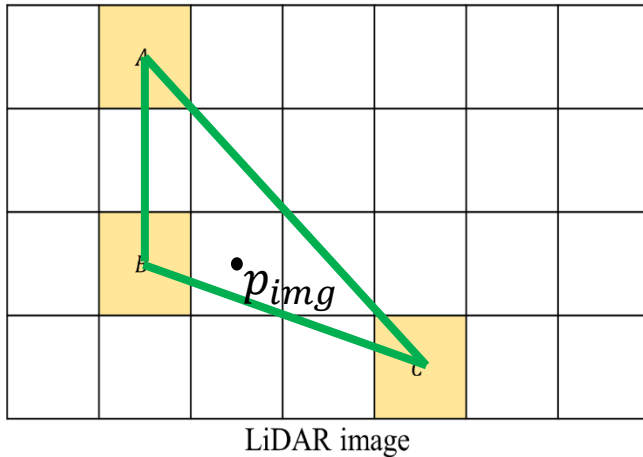
- Plane interpolation



# Interpolation

- Method 3

- Plane interpolation



$$\text{line } AB : y = a_{AB} * x + b_{AB}$$

$$\text{line } BC : y = a_{BC} * x + b_{BC}$$

$$\text{line } CA : y = a_{CA} * x + b_{CA}$$

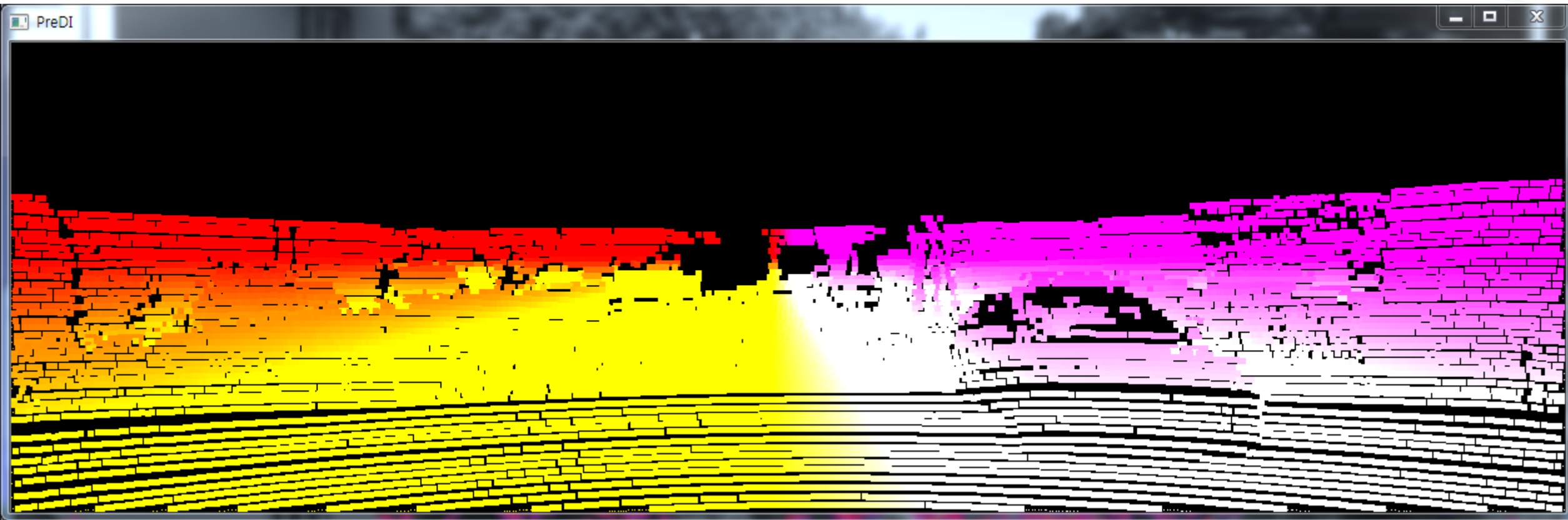
*valid function:*

$$\text{if } (p_{img_y} - a_{AB} * p_{img_x} + b_{AB}) * (C_y - a_{AB} * C_x + b_{AB}) < 0, \text{ continue;}$$

$$\text{if } a_{AB} = \infty, \quad \left( (A \text{ or } B)_x - p_{img_x} \right) * \left( (A \text{ or } B)_x - C_x \right) < 0, \text{ continue;}$$

# Result

- LiDAR data – dilation interpolation





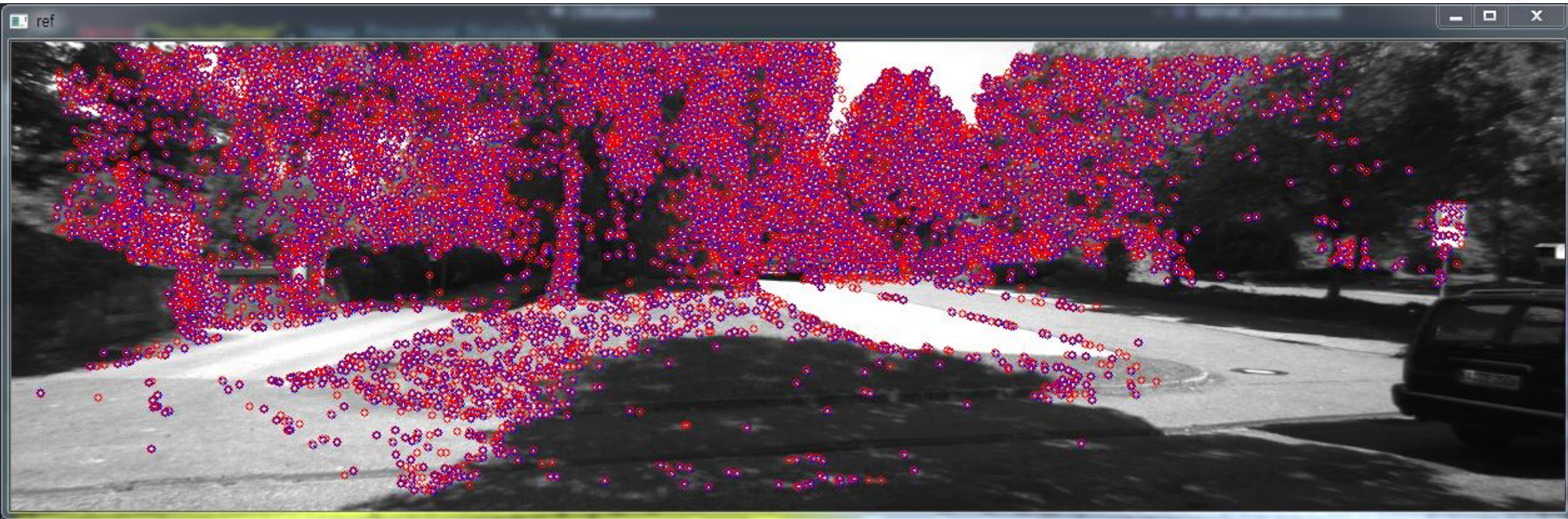
# Result

- Reprojection error – dilation interpolation



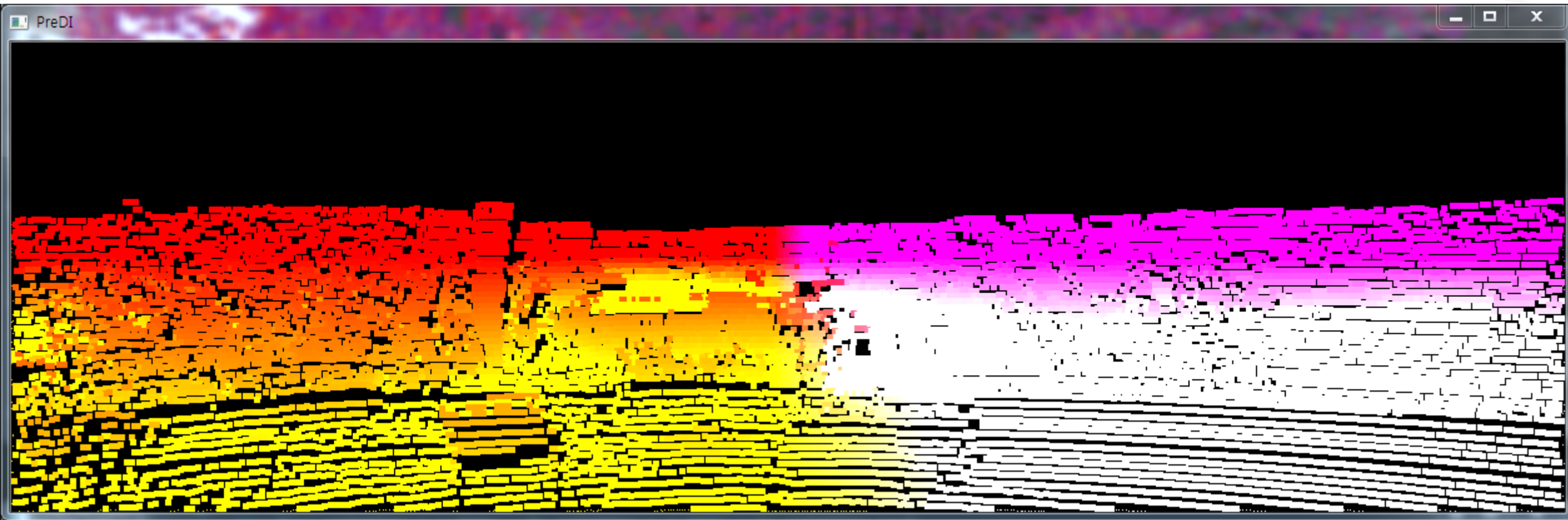
# Result

- Reprojection error – dilation interpolation



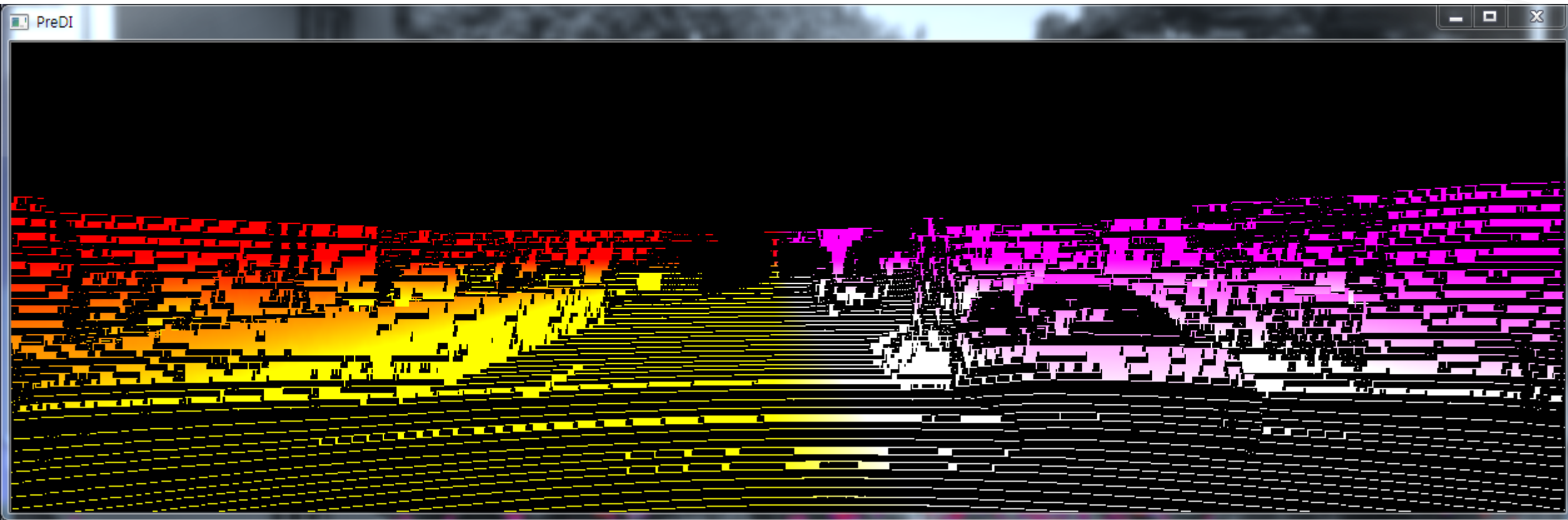
# Result

- Outlier



# Result

- LiDAR data – adaptive bilinear interpolation



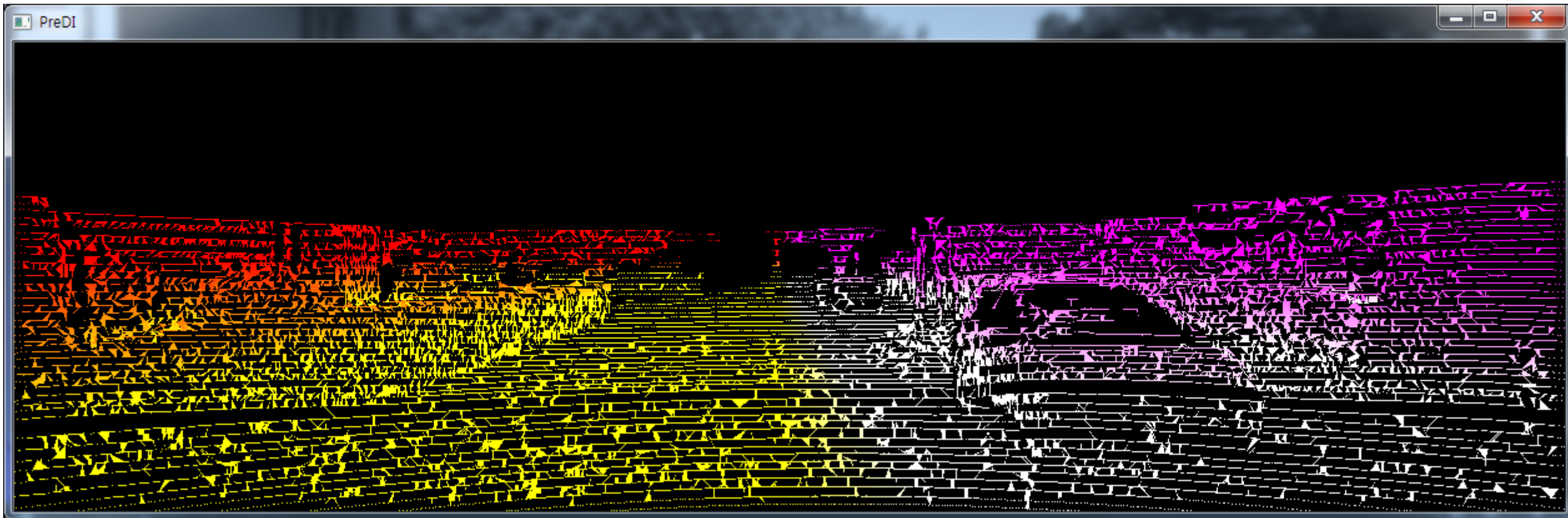
# Result

- Reprojection error – adaptive bilinear interpolation



# Result

- LiDAR data – plane interpolation



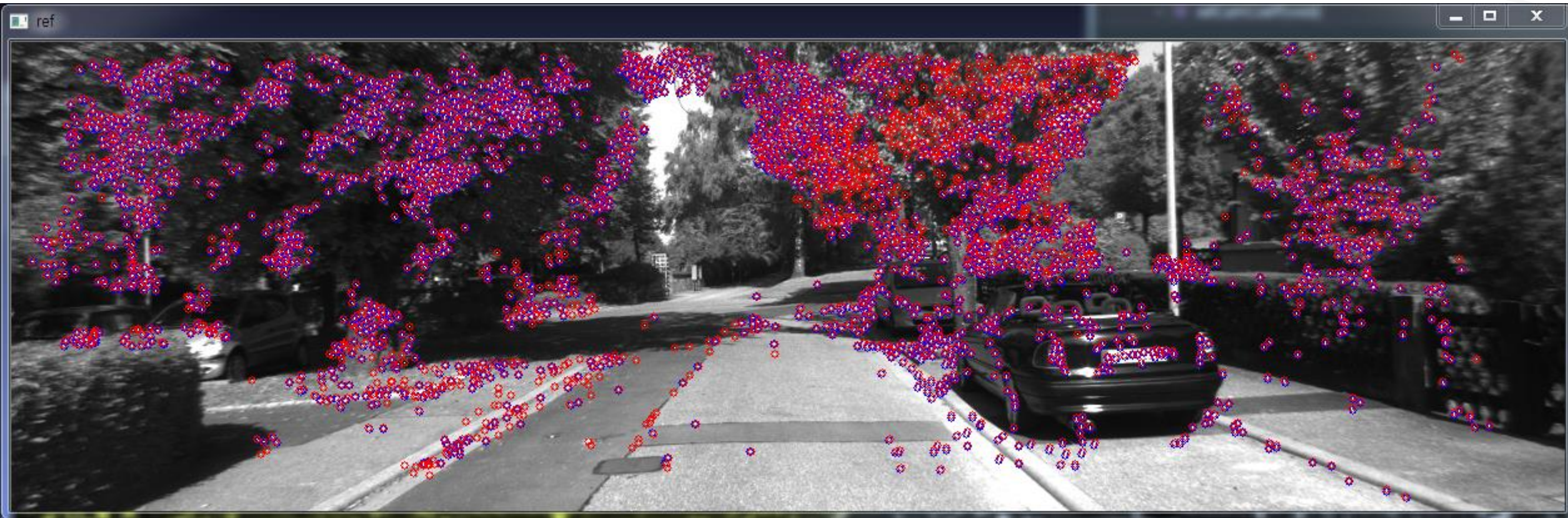
# Result

- Reprojection error - plane interpolation



# Result

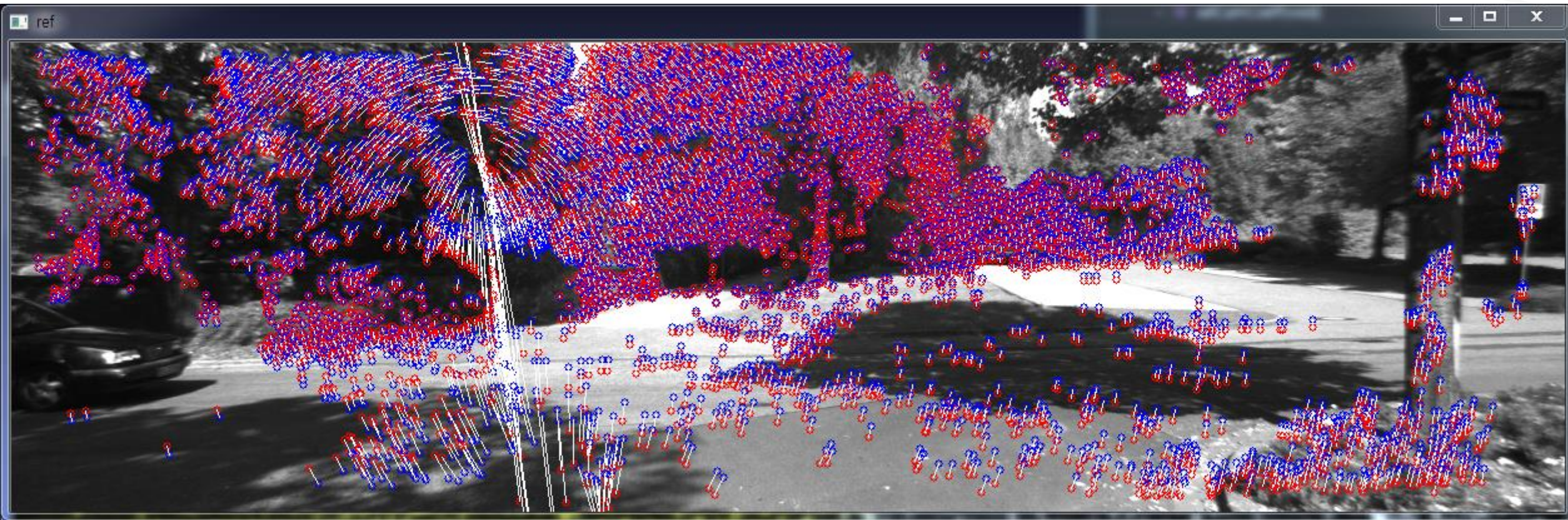
- Reprojection error - plane interpolation





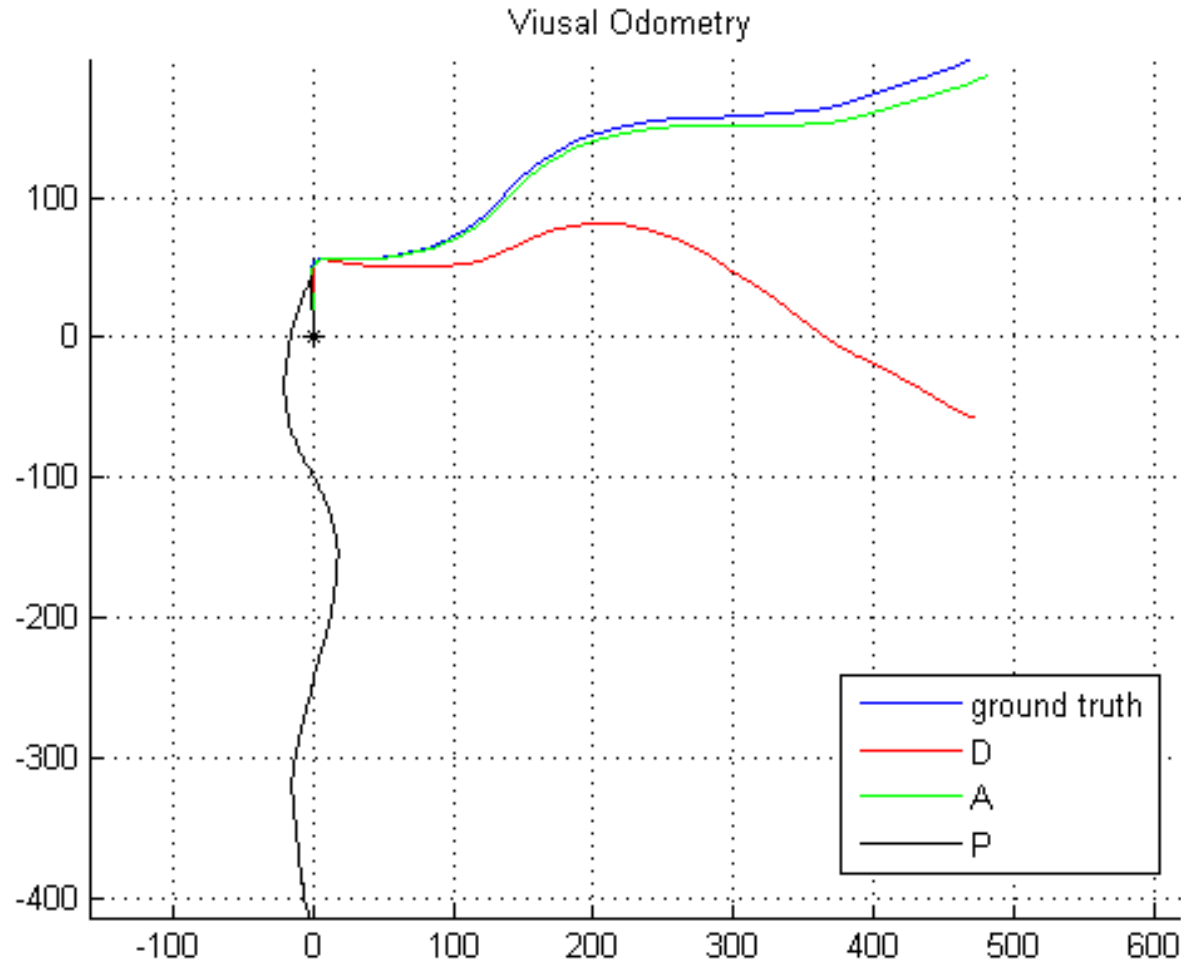
# Result

- Reprojection error - plane interpolation









# Result

- Visual Odometry



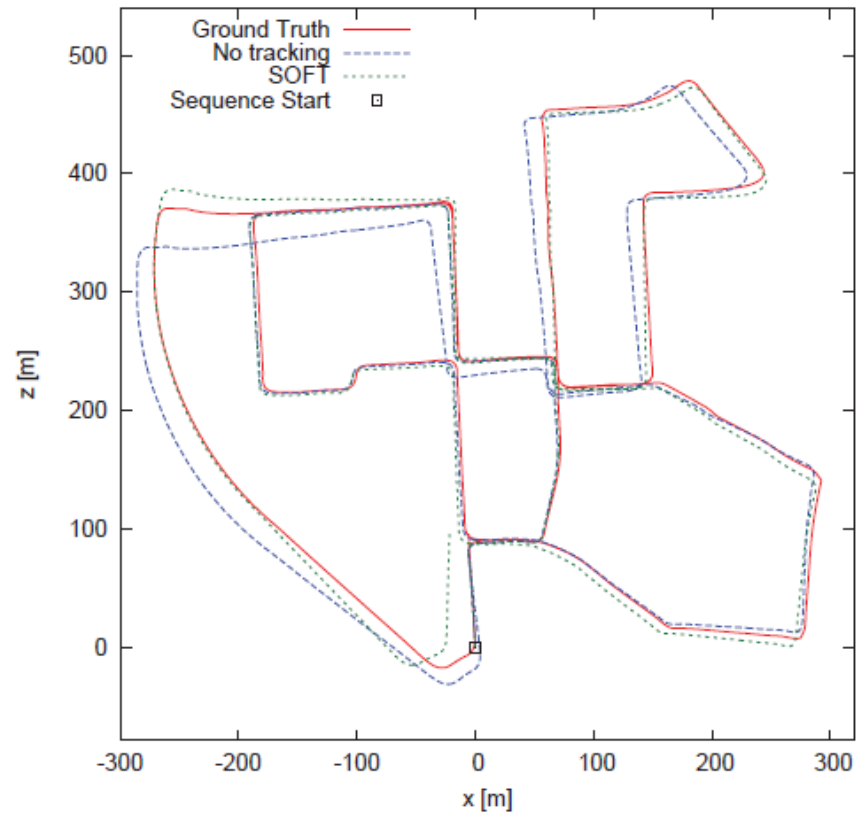
# Conclusion

- SOFT (Stereo Odometry based on careful feature selection and tracking)

	Method	Setting	Code	Translation	Rotation	Runtime	Environment	Compare
1	<a href="#">V-LOAM</a>			0.68 %	0.0016 [deg/m]	0.1 s	2 cores @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
J. Zhang and S. Singh: <a href="#">Visual-lidar Odometry and Mapping: Low drift, Robust, and Fast</a> . IEEE International Conference on Robotics and Automation(ICRA) 2015.								
2	<a href="#">LOAM</a>			0.70 %	0.0017 [deg/m]	0.1 s	2 cores @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
J. Zhang and S. Singh: <a href="#">LOAM: Lidar Odometry and Mapping in Real-time</a> . Robotics: Science and Systems Conference (RSS) 2014.								
3	<a href="#">SOFT2</a>			0.81 %	0.0022 [deg/m]	0.1 s	2 cores @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
4	<a href="#">GDVO</a>			0.86 %	0.0031 [deg/m]	0.09 s	1 core @ >3.5 Ghz (C/C++)	<input type="checkbox"/>
5	<a href="#">HypERROCC</a>			0.88 %	0.0027 [deg/m]	0.25 s	2 cores @ 2.0 Ghz (C/C++)	<input type="checkbox"/>
6	<a href="#">SOFT</a>			0.88 %	0.0022 [deg/m]	0.1 s	2 cores @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
I. Cvišić and I. Petrović: <a href="#">Stereo odometry based on careful feature selection and tracking</a> . European Conference on Mobile Robots (ECMR) 2015.								

# Conclusion

- SOFT (Stereo Odometry based on careful feature selection and tracking)



Reconstructed path of the KITTI00 dataset



Stereo camera with IMU

# Conclusion

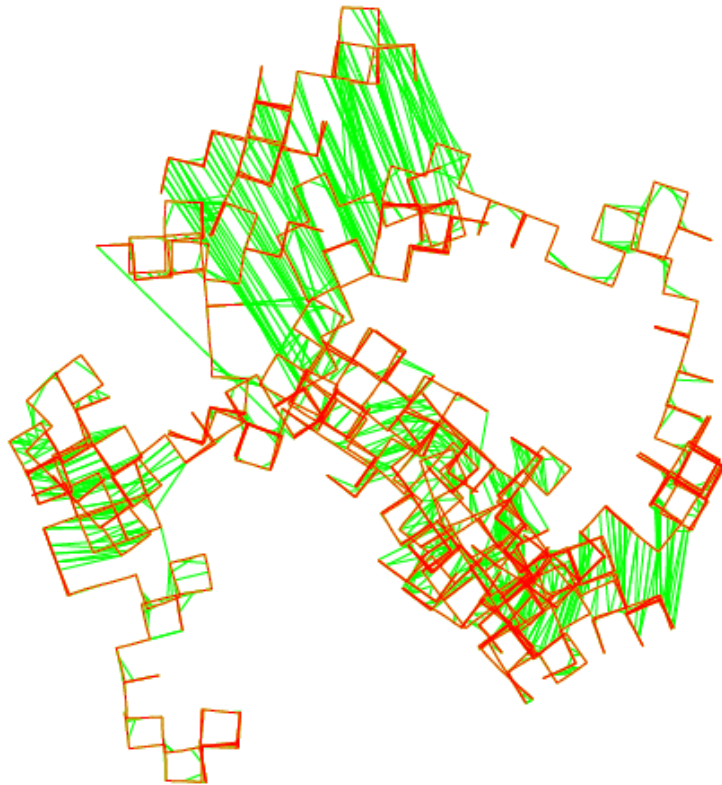
- SOFT (Stereo Odometry based on careful feature selection and tracking)



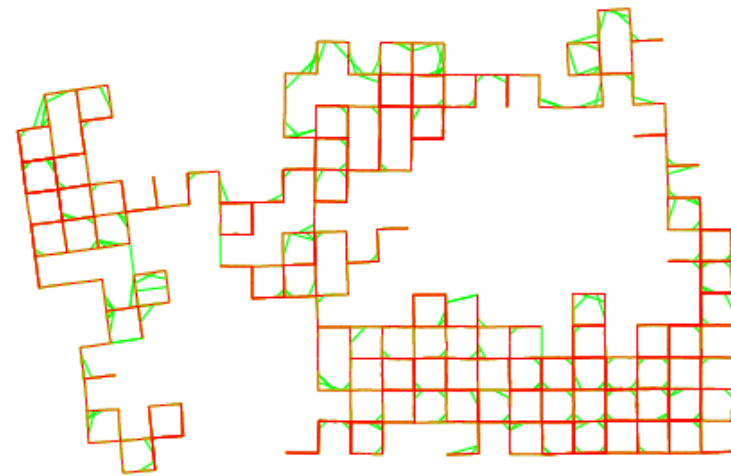
Path estimated from self recorded dataset

# Conclusion

- Optimization – iSAM (Incremental Smoothing and Mapping)



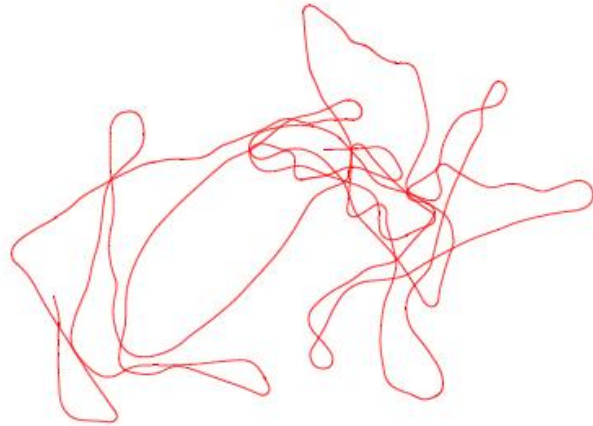
(a) Original noisy data set.



(b) Trajectory after incremental optimization.

# Conclusion

- Optimization – iSAM (Incremental Smoothing and Mapping)



(a) Trajectory based on odometry only.



(b) Trajectory and map after incremental optimization.

# Q&A